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Journal of Fluid Mechanics

Volume 686

Page range 352-377

Year 2011

URL http://id.nii.ac.jp/1476/00005579/


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<td>10.1017/jfm.2011.334(<a href="http://dx.doi.org/10.1017/jfm.2011.334">http://dx.doi.org/10.1017/jfm.2011.334</a>)</td>
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DOI: 10.1017/jfm.2011.334, Published online: 22 September 2011

Link to this article: http://journals.cambridge.org/abstract_S002211201100334X

How to cite this article:

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Streamwise variation of turbulent dynamics in boundary layer flow of drag-reducing fluid

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(Received 28 January 2011; revised 1 July 2011; accepted 1 August 2011; first published online 22 September 2011)

Direct numerical simulations (DNSs) of a zero-pressure-gradient boundary layer flow of a polymeric fluid have been performed. The FENE-P model was used for the polymer stresses and a wide range of Weissenberg numbers (We) was addressed. In all cases, the streamwise variations of the level of polymer stretching and the level of drag reduction are anticorrelated. Consistent with earlier studies, the inlet condition for the flow consists of Newtonian velocity data with no polymer stretching, so in the upstream region of the boundary layer the polymer molecules stretch strongly in response, leading to an initial spatial maximum in polymer stretching. Beyond this initial region, the level of drag reduction increases with increasing downstream position, while the polymer stretch is decreasing. At sufficiently high Weissenberg numbers, these variations are monotonic with streamwise position (outside the upstream region), but at We = 25, both the polymer stretching and level of drag reduction display a decaying oscillation in the downstream position. The streamwise dependence of the velocity statistics is also shown. In addition, simulations in which the polymer stress is turned off beyond a chosen downstream position were performed; in this case the flow continues to exhibit substantial drag reduction well downstream of the cutoff position. These observations are analysed in light of other recent literature and in particular the observations of ‘active’ and ‘hibernating’ turbulence recently found in minimal channel flow by Xi and Graham. All of these observations suggest that an important role for viscoelasticity in the turbulent drag reduction phenomenon, at least near solid surfaces, is to suppress conventional turbulence, while leaving behind a much weaker form of turbulence that can persist for a substantial length of time (or downstream distance) even in the absence of viscoelastic stresses.

Key words: drag reduction, polymers, turbulent boundary layers

1. Introduction

It is well known that significant drag reduction can be observed for wall-bounded turbulent flows of viscoelastic fluids such as dilute polymer and surfactant solutions. A key result in the literature of drag reduction was obtained by Virk (1975) who noted the existence of a parameter regime called the maximum drag reduction

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(MDR) asymptote. In this regime the mean velocity profile has a log-law region with a distinct slope that is universal with respect to molecular weight, concentration, polymer species, and pipe diameter. It has been reported that in the MDR regime the Reynolds shear stress substantially decreases (Warholic, Massah & Hanratty 1999a; Warholic, Schmidt & Hanratty 1999b). The Virk mean velocity profile in the MDR regime has been reproduced by direct numerical simulations (DNSs) of drag-reducing turbulent channel flow of polymer solutions (e.g. Ptasinski et al. 2003; Dubief et al. 2005; Li, Sureshkumar & Khomami 2006).

However, despite numerous efforts in this field (e.g. Virk 1975; Sreenivasan & White 2000; Benzi, De angelis & L’vov 2006; Procaccia, L’vov & Benzi 2008), understanding of MDR remains largely phenomenological or empirical (White & Mungal 2008). Since the pioneering papers of Sureshkumar, Beris & Handler (1997) and Dimitropoulos et al. (2005) on the DNS of the drag-reducing channel flow and boundary layer, respectively, numerous DNS studies have been performed to investigate the viscoelastic wall-bounded turbulent flows using constitutive equation models such as the finitely extensible nonlinear elastic Peterlin (FENE-P) model, Oldroyd-B model and Giesekus model (Bird, Armstrong & Hassager 1987a,b). As reported in the review of White & Mungal (2008), these studies can predict some experimental findings such as a steeper gradient of the mean velocity profile in wall units and more suppression of wall-normal turbulence intensity and Reynolds shear stress with the amount of the drag reduction, and have revealed the effect of viscoelastic stress on velocity fields.

More specifically, DNS studies on drag-reducing turbulent channel flows indicate that the elongational viscosity and Weissenberg number are key parameters for the drag reduction (e.g. Dimitropoulos, Sureshkumar & Beris 1998; Housiadas & Beris 2004; Li et al. 2006; Yu & Kawaguchi 2003, 2006). At a constant Weissenberg number, moreover, Tamano et al. (2009a) performed DNS of the drag-reducing turbulent boundary layer in viscoelastic fluids using the Oldroyd-B, Giesekus and FENE-P models, and clarified the effects of rheological properties such as the elongational and shear viscosities, and the first and the second normal stress differences on the drag reduction. Owing to these macroscopic approaches, substantial new knowledge on the relation between the drag reduction and rheological properties of viscoelastic solutions such as the relaxation time and elongational viscosity has been obtained. In terms of relation between polymer stress and turbulence structures, moreover, many researchers showed that polymer stresses counteract near-wall streamwise vortices (e.g. De Angelis, Casciola & Piva 2002; Stone, Waleffe & Graham 2002; Stone et al. 2004; Dubief et al. 2004, 2005; Li & Graham 2007; Kim et al. 2007, 2008). However, how polymers or surfactant micelles interact with near-wall turbulence structure, especially as the level of drag reduction approaches the MDR regime, remains poorly understood.

Xi & Graham (2010a,b) have recently studied Newtonian and viscoelastic turbulent dynamics in a minimal channel flow geometry. A number of the observations from that study are relevant to the present work. The main overall observation Xi & Graham (2010b) was the existence of time intervals of what they called ‘hibernating’ turbulence, during which the polymer stresses decreased while the mean velocity was increasing. During hibernation, the instantaneous mean velocity profile approached a log-law with a slope approaching that found in the MDR regime, and the Reynolds shear stresses, streamwise vortex strength and streamwise variation of the flow field all dropped to low values. Under the conditions considered, these hibernation intervals last about five eddy turnover times, after which the turbulence reverts to a more
conventional, ‘active’ state. As the Weissenberg number increases, the active intervals
become shorter, while the hibernating intervals remain approximately the same length.
Thus, a key result of this paper is that in the minimal channel, the instantaneous
levels of polymer stretching and drag reduction are anticorrelated in time: during the
active turbulence intervals, the polymers become highly stretched and the resulting
stresses suppress the active turbulence, driving the flow into hibernation. During
hibernation, the turbulence is very weak and does not stretch the polymer molecules,
which therefore relax. The hibernating turbulence is unstable and eventually new
three-dimensional turbulent fluctuations grow, moving the turbulence back into the
active regime. Finally, another key result of this study was that intervals of hibernation
displaying the Virk slope are observed even in the limit of zero Weissenberg number:
Newtonian flow. One key goal of the present work is to determine to what extent
the anticorrelation of polymer stretching and drag reduction observed in the minimal
channel results is found in boundary layer turbulence.

There is some existing evidence that this scenario is relevant, with time replaced
with downstream position, for boundary layer flow. Dimitropoulos et al. (2005) found
that drag reduction increases as polymer extension decreases. Dimitropoulos et al.
(2005) and Hou, Somandepalli & Mungal (2008) also proposed that in the steady-state
region, the reduced turbulent intensity allowed the polymer to be less stretched and
still maintained a high drag reduction, so that the polymer stress was not necessarily
high. As reported by Hou et al. (2008), the dependence of turbulence intensity of the
velocity fluctuations on the drag reduction ratio is more complex compared with the
turbulent channel flow. Very recently, Dubief et al. (2011) observed, in a simulation
of Newtonian boundary layer flow, that at a spatial position just upstream of where
streamwise vortices and turbulent spots form the mean velocity profile looks strikingly
similar to the Virk MDR profile. This observation is further evidence of the transient
presence of MDR-like dynamics in Newtonian flow.

In the present study, we perform DNS of a zero-pressure gradient turbulent
boundary layer of a drag-reducing homogeneous viscoelastic fluid with the FENE-P
model at Weissenberg numbers up to $We = 100$, and investigate the effects of $We$
on streamwise variations in turbulence statistics and structures in the turbulent boundary
layer. Although there have been some past comparisons of turbulence statistics at
$We = 25$ and 50 for the boundary layer (see Dimitropoulos et al. 2005; Tamano et al.
2009a), the literature on the effect of $We$ on turbulence structures is very limited in
comparison to channel flow. In particular, the modification of streamwise variations
remains unknown. In the present study, the streamwise computational domain is
enlarged by a factor of two compared with our previous DNS at $We = 25$ (Tamano et al.
2007). A particular focus of this work is the evaluation of the results in light of
the observations of active and hibernating turbulence in channel flow and their
relevance in the more complex case of boundary layer flow.

The present paper is arranged as follows. The fundamental equations and numerical
methods are presented in §§ 2 and 3. In § 4, numerical simulation results are presented.
First, the effect of $We$ on turbulence statistics and their streamwise variations are
investigated. Next, the joint probability density functions of instantaneous wall-shear
stress (or trace of conformation tensor) and streamwise velocity scaled by friction
velocity at a constant wall-normal position are discussed. Finally, the results of
additional numerical simulations at $We = 100$ with a damping function which makes
all components of conformation tensor zero in the downstream region are presented in
order to clarify the role of conformation tensor. Throughout, we assess the relevance of
the active–hibernating picture for the boundary layer flow. Key results are summarized and conclusions are given in § 5.

2. Formulation

The non-dimensional continuity and momentum equations for incompressible viscoelastic flow are

$$\frac{\partial u_i}{\partial x_i} = 0,$$

(2.1)

$$\frac{\partial u_i}{\partial t} + \frac{\partial u_i u_j}{\partial x_j} = - \frac{\partial p}{\partial x_i} + \frac{1 - \beta}{Re_{\theta_0}} \frac{\partial E_{ij}}{\partial x_i} + \frac{\beta}{Re_{\theta_0}} \frac{\partial^2 u_i}{\partial x_j \partial x_j},$$

(2.2)

where $u_i$ is the velocity component, $p$ is pressure, $x_i$ is a spatial coordinate, $t$ is time and $E_{ij}$ is the viscoelastic stress component. In this paper, $x_1$ ($x$), $x_2$ ($y$) and $x_3$ ($z$) directions are streamwise, wall-normal and spanwise, respectively. In the present study, the non-dimensional computational parameters are the momentum–thickness Reynolds number $Re_{\theta_0}$ and the Weissenberg number $We$, which are defined as follows:

$$Re_{\theta_0} = \frac{\rho U_e \theta_0}{\eta_0},$$

(2.3)

$$We = \frac{\lambda U_e}{\theta_0},$$

(2.4)

where $U_e$ is the free stream velocity, $\theta_0$ is the momentum–thickness at the inlet plane of the driver part, $\rho$ is density and $\lambda$ is the relaxation time. The ratio of solvent viscosity $\eta_s$ to zero shear rate solution viscosity $\eta_0$ is $\beta$. The non-dimensional FENE-P constitutive equation for the conformation tensor $C_{ij}$ is as follows (Bird et al. 1987b):

$$\frac{\partial C_{ij}}{\partial t} + u_k \frac{\partial C_{ij}}{\partial x_k} - \frac{\partial u_i}{\partial x_k} C_{kj} - \frac{\partial u_j}{\partial x_k} C_{ik} = -E_{ij}.$$  

(2.5)

The viscoelastic stress is related to the conformation tensor as

$$E_{ij} = \frac{f C_{ij} - \delta_{ij}}{We},$$

(2.6)

where the Peterlin function $f$ is defined by

$$f = \frac{L^2}{L^2 - \text{Tr}(C_{ij})},$$

(2.7)

and $L$ represents the maximum extension of the polymer. For the FENE-P model, the extensibility parameter $Ex$ is given by

$$Ex = \frac{2L^2(1 - \beta)}{3\beta}.$$  

(2.8)

This is the maximum value of the ratio between polymeric and viscous contributions to extensional viscosity (Trouton ratio). Only when the extensibility parameter $Ex$ is much larger than unity are significant effects of the polymer on turbulence expected. In the present study, in which $\beta$ and $L^2$ are fixed at 0.9 and 10 000, respectively, the value of $Ex$ is 740.74.

In this study, the inflow condition for the boundary layer is given by the method proposed by Lund, Wu & Squires (1998), so that the computational domain is divided
into the main part and driver part from which the inflow condition for the main part is obtained. This approach was also used in prior studies (Dimitropoulos et al. 2005, 2006; Tamano et al. 2007, 2009a). The inlet boundary condition is discussed further in the next section.

3. Numerical method and conditions

The second-order accurate finite difference scheme on a staggered grid is used. The velocity components are discretized on the grid cell edges, whereas the pressure and all components of the viscoelastic stress tensor $E_{ij}$ and conformation tensor $C_{ij}$ are defined at the centre of each cell. The coupling algorithm of the discrete continuity and momentum equations (2.1) and (2.2) is based on the second-order splitting method (Dukowicz & Dvinsky 1992). The resulting discrete Poisson equation for the pressure is solved by the Bi-CGSTAB (bi-conjugate gradients stabilized) method (Van Der Vorst 1992) after fast Fourier transform (FFT) in the periodic ($z$) direction. The second-order upwind difference scheme is used for the polymer-stress convection term $u_k \partial C_{ij} / \partial x_k$ in (2.5). An artificial diffusion term $1/(ScRe_\theta) \partial^2 C_{ij} / \partial x_j^2$ is added in (2.5) to prevent numerical instability, where $Sc = \eta_0 / (\rho D)$ is the Schmidt number and $D$ is an artificial stress diffusion coefficient for polymer. (Using the actual, very small value of the molecular diffusivity would not lead to stabilization.) The semi-implicit time marching algorithm is used where the diffusion term in the wall-normal direction is treated implicitly with the Crank–Nicolson scheme, and the third-order Runge–Kutta scheme is used for all other terms.

The non-slip boundary condition ($u = v = w = 0$) is applied on the wall. The boundary conditions on the top surface of the computational domain are $\partial u / \partial y = 0$, $v = U_e \delta^* / d_x$, and $\partial w / \partial y = 0$, where $\delta^*$ is the boundary layer displacement thickness. Periodic boundary conditions for the velocity and viscoelastic stress components are imposed in the spanwise direction. A convective boundary condition, $\partial u_i / \partial t + U_e \partial u_i / \partial x = 0$, is used at the outlet plane. The inflow condition is generated using the recyle method of Lund et al. (1998) as mentioned above. This is because otherwise, a very long streamwise computational domain would be necessary to capture the spatially developing boundary layer flow including the laminar to turbulent transition Wu & Moin (2009). Simulating this entire region would be extremely computationally expensive. In the present study, the velocity field data at the streamwise centre of the driver part provide inflow data at the inlet of the main part. The present inlet boundary conditions are the same as those of previous studies (Dimitropoulos et al. 2005, 2006; Tamano et al. 2007, 2009a). The boundary conditions for the viscoelastic stress components are given by solving the constitutive equations at the wall with the velocity boundary conditions satisfied, except for the inlet boundary of the main part at which all of the viscoelastic stress components $E_{ij}$ are fixed at zero, i.e. the Newtonian velocity data are imposed directly. It is known that this type of inlet boundary condition has consequences for the predicted level of the drag reduction and the polymer conformation state near the inlet region. In particular, the polymer molecules stretch rapidly from their equilibrium state and the resulting large extensional viscosity leads to an initial increase in drag relative to the Newtonian flow, and thus to a negative level of drag reduction (see figures 3 and 10b). Physically, the imposed inlet condition is somewhat analogous to injecting the polymer into a boundary layer at a finite distance downstream from the leading edge.

In the present study, the momentum–thickness Reynolds number $Re_\theta$ is 500 and the Weissenberg number $We = 25$, 50, 75 and 100 (see table 1). The size of the
Table 1. Numerical and physical conditions.

<table>
<thead>
<tr>
<th></th>
<th>We</th>
<th>β</th>
<th>$L^2$</th>
<th>$\Delta t U_e/\theta_0$</th>
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<td>Newtonian</td>
<td>1.0</td>
<td>1.0</td>
<td>10000</td>
<td>0.008</td>
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<tr>
<td>FENE-P</td>
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<td>0.9</td>
<td>10000</td>
<td>0.008</td>
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Table 2. Residence and integral time versus relaxation time.

<table>
<thead>
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<th>We</th>
<th>$T_{\text{residence}}/\lambda$</th>
<th>$T_{\text{integral}}/\lambda$</th>
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<tr>
<td>25</td>
<td>16.0</td>
<td>80</td>
</tr>
<tr>
<td>50</td>
<td>8.0</td>
<td>40</td>
</tr>
<tr>
<td>75</td>
<td>5.3</td>
<td>27</td>
</tr>
<tr>
<td>100</td>
<td>4.0</td>
<td>20</td>
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The computational domain for the present simulations is equal to $(L_x \times L_y \times L_z) = (400\theta_0 \times 30\theta_0 \times 20\pi\theta_0/3)$ in the streamwise, wall-normal and spanwise directions, respectively. The grid size is $(N_x \times N_y \times N_z) = (512 \times 64 \times 64).$ The grid spacing in $x$ and $z$ directions is uniform, and the wall-normal grids are given by a hyperbolic tangent stretching function. The present spatial resolution is $(\Delta x^+|_{\text{inlet}}, \Delta y^+|_{\text{inlet}} = \Delta y^+|_{\text{inlet}} = (20, 0.38–37, 8.5)$ for both Newtonian and the FENE-P model, which is somewhat larger than that of previous DNSs (Dimitropoulos et al. 2005, 2006) for the corresponding drag-reducing turbulent boundary layer with the same spatial discretization method. Recent high-resolution spectral DNSs for Newtonian flows showed surprisingly large differences in both basic integral quantities such as the friction coefficient and the shape factor, and revealed that the numerical simulation of turbulent boundary layers was, mainly due to the spatial development of the flow, very sensitive to, for example, proper inflow condition, sufficient settling length and appropriate box dimensions (see Schlatter & Örlü 2010). The present numerical grid resolution is not enough to compare quantitatively such recent spectral DNS results for Newtonian flows, but it is not expected to affect the qualitative conclusions obtained in the present study on the drag-reducing effects (see also § 4.1 for details). The streamwise and spanwise computational sizes in wall units at the inlet are $L_x^+|_{\text{inlet}} = 1.0 \times 10^4$ and $L_z^+|_{\text{inlet}} = 5.5 \times 10^2$, respectively. Here, the ratios of present residence time in the computational domain, $T_{\text{residence}} = L_x/U_e$, and integral time for ensemble average of turbulence statistics $T_{\text{integral}}$ to the relaxation time $\lambda$ are presented in Table 2. Even at $We = 100$, the residence time is a factor of four larger than the relaxation time. For all of the cases, the present integral time is much larger than the relaxation time.

In the driver part, the computational domain and grid size are $(100\theta_0 \times 30\theta_0 \times 20\pi\theta_0/3)$ and $(128 \times 64 \times 64)$, respectively. The present turbulence statistics are obtained by averaging over space (spanwise direction) and time of over 2000$\theta_0/U_e$ after the turbulent flow becomes stationary, where the time increment $\Delta t U_e/\theta_0$ is 0.008 for the FENE-P model and 0.02 for Newtonian fluid. In this paper, $-'-$ represent the time–space (spanwise direction) average and the deviation, respectively. The superscript $+$ represents the spanwise- and time averaged local variables normalized by wall variables. The superscript $++$ represents values scaled by inner variables.
Newtonian
Newtonian
Newtonian
Newtonian
10
15
20
100 200 300
0 100 200 300 400
1.0
1.5
2.0
We = 100
We = 75
We = 50
We = 25
We = 75
We = 50
We = 25
We = 75
We = 100
0 100 200 300 400
(a)
(b)
(c)
(d)

Figure 1. Streamwise variations in (a) boundary layer thickness $\delta/\theta_0$, (b) momentum thickness $\bar{\delta}/\theta_0$, (c) displacement thickness $\delta^*/\theta_0$, (d) wall-shear stress $\tau_w/\rho U_e^2$.

4. Results

4.1. Boundary layer parameters and drag reduction ratio

Figures 1(a)–(d) show the streamwise variations in boundary layer thickness $\delta/\theta_0$, momentum thickness $\bar{\delta}/\theta_0$, displacement thickness $\delta^*/\theta_0$, and wall-shear stress $\tau_w/\rho U_e^2$, respectively. The streamwise development of $\delta/\theta_0$ is suppressed more with the increase in $We$, and $\bar{\delta}/\theta_0$ at $We = 75$ and 100 are almost identical. The value of $\bar{\delta}/\theta_0$ at $We = 50$–100 is strongly suppressed, while at $We = 25$ it is between the Newtonian and higher $We$ cases. The value of $\delta^*/\theta_0$ at $We = 50$–100 is larger in the downstream region compared with the Newtonian fluid, while at $We = 25$ it is smaller than that for the Newtonian fluid. The behaviour of $\bar{\delta}/\theta_0$ and $\delta^*/\theta_0$ is directly related to the shape factor $H = \delta^*/\theta$ (see figure 2a later). At $We = 50$–100, the wall shear stress $\tau_w/\rho U_e^2$ increases near the inlet region and monotonically decreases, while at $We = 25$, $\tau_w/\rho U_e^2$ oscillates in the downstream region, in which its value is still smaller than that of Newtonian fluid. The $\tau_w/\rho U_e^2$ corresponds to the friction
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Figure 2. Boundary layer development: (a) shape factor versus Reynolds number and (b) friction coefficient versus momentum–thickness Reynolds number.

Figure 3. Streamwise variation in drag reduction ratio.

coefficient \( C_f = \tau_w/\left(\rho U_e^2/2\right) \) (see figure 2b), and this behaviour is closely related to the drag reduction ratio (see figure 3).

Figures 2(a) and 2(b) show the dependence of the shape factor \( H \) and skin friction coefficient \( C_f \) on the momentum–thickness Reynolds number \( Re_\theta \), which is useful for comparison with experimental data. In these figures, the solid and dotted lines represent Coles’ curves (Coles 1962) and DNS data obtained by Spalart (Spalart 1988), respectively. The data of \( H \) for Newtonian fluid agree well with Coles’ curves and DNS data of Spalart, while the data of \( C_f \) is somewhat larger. This may be due to the effect of grid resolution as mentioned in § 3. However, the trend of \( C_f \) is consistent with the Coles’ curves and the value is within a 10% tolerance. It should be noted that even in the spectral DNS of Newtonian flows, it is not only the actual values of \( C_f \) that differ, but also inconsistent trends with respect to \( Re_\theta \) (see Schlatter & Örlü 2010).

As the Reynolds number increases, the value of \( H \) at \( We = 25–100 \) first decreases near the inlet region, and then drastically increases from \( Re_\theta \simeq 650 \) to the outlet plane (figure 2a). The increase in \( H \) versus \( Re_\theta \) observed here is consistent with the previous experimental study on the drag-reducing turbulent boundary layer flow in cationic and non-ionic surfactant solutions (see Itoh et al. 2005; Tamano et al. 2009b, 2010).

It should be noted that at \( We = 25 \), \( H \) oscillates in the downstream region, and at
We $= 50$, it has a maximum around $Re_\theta = 800$. The value of $C_f$ increases with the increase in $Re_\theta$ for $Re_\theta \lesssim 650$, after the maximum it decreases. At $We = 25$, $C_f$ oscillates in the streamwise direction. The behaviour of $C_f$ is consistent with that of $H$. The comparison of $C_f$ with Newtonian fluid is discussed by estimating the drag reduction ratio (see figure 3).

Figure 3 shows the streamwise variation in the drag reduction ratio $DR$ for the four values of $We$ studied here. This ratio is defined as follows:

$$DR(x) = \frac{C_{f,\text{Newtonian}}(x) - C_{f,\text{Viscoelastic}}(x)}{C_{f,\text{Newtonian}}(x)},$$

(4.1)

where $C_{f,\text{Newtonian}}(x)$ and $C_{f,\text{Viscoelastic}}(x)$ are the skin friction coefficients for Newtonian and viscoelastic fluids, which are functions of the streamwise position $x$. The drag-reducing effect shifts downstream with the increasing $We$. It can be concluded that the streamwise profile of $DR$ shifts downstream with the increase in the relaxation time, since the other rheological parameters and the Reynolds number are constant. The level of $DR$ at $We = 25$ is much smaller than those of $We = 50$ and higher, which is consistent with the previous DNSs (Dimitropoulos et al. 2005; Tamano et al. 2009a). At $We = 50–100$, the $DR$ becomes larger in the streamwise direction, and seems to saturate at more than 60%. On the other hand, at $We = 25$, the region of $DR$ is below ~40%, and oscillates with downstream position: the first maximum is at $x/\theta_0 \simeq 150$, the minimum is at $x/\theta_0 \simeq 260$, and a second slight maximum is at $x/\theta_0 \simeq 380$.

In the inlet region, the negative $DR$ is due to the sudden change of velocity fields caused by the unrealistic effect of the inlet boundary condition in which the velocity field data of Newtonian fluid in the driver part are used directly (see Dimitropoulos et al. 2005, 2006; Tamano et al. 2007, 2009a).

4.2. Turbulence statistics

Figure 4(a–d) show the wall-normal profiles of mean (spanwise and time averaged) velocity, $U^+$, at different streamwise locations. In these figures, the linear profile $U^+ = y^+$, the log-law profile ($U^+ = 2.44 \ln y^+ + 5.0$) and the Virk ultimate profile (Virk 1975) ($U^+ = 11.7 \ln y^+ - 17$) are also shown. At $We = 25$, $U^+$ shifts upward compared with the Newtonian log-law. On the other hand, at $We = 50$ and higher, $U^+$ shifts upward more and increases with the increase in $x$, i.e. the increase in $DR$, and the slope is much larger than that of the Newtonian log-law. The present DNS results are consistent with previous experiments (e.g. Warholic et al. 1999a; Itoh et al. 2005; Tamano et al. 2009b) and DNS (e.g. Dimitropoulos et al. 2005; Tamano et al. 2009a). At $We = 75$ and 100, the mean velocities at $x/\theta_0 = 392.2$ agree well with the Virk ultimate profile.

Figure 5 shows profiles of streamwise turbulence intensity, $u_{rms}^+$, at $We = 25–100$. At $We = 25$, except in the upstream region where the $DR$ is negative, $u_{rms}^+$ is larger than that from the DNS by Spalart (1988) for Newtonian fluid, and the maximum becomes larger in the streamwise direction. The wall-normal location of the maximum is slightly farther from the wall. At $We = 50$, the maximum of $u_{rms}^+$ in the downstream region is much larger than that of the Newtonian fluid, over 1.5 times larger at $x/\theta_0 = 392.2$. At $We = 75$, the maximum of $u_{rms}^+$ (outside the upstream region) becomes larger in the streamwise direction, as in the case of $We = 50$, but the maxima near the wall are much smaller compared with those of $We = 50$, and the plateau region appears around $y^+ = 100$, which is not detected in $We = 25$ and 50. At $We = 100$, the streamwise turbulence intensity is strongly attenuated across the boundary layer (figure 5d), and the maximum of $u_{rms}^+$ shows somewhat complex
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\[ U^+ = 11.7 \ln y^+ - 17 \]

We = 25 Newtonian
\[ x/\theta_0 = 88.28 \quad \bullet \]
\[ x/\theta_0 = 200.0 \quad \triangle \]
\[ x/\theta_0 = 300.0 \quad \square \]
\[ x/\theta_0 = 392.2 \quad \diamond \]
\[ U^+ = y^+ \]
\[ U^+ = 2.44 \ln y^+ + 5.0 \]

We = 50 Newtonian
\[ x/\theta_0 = 88.28 \quad \bullet \]
\[ x/\theta_0 = 200.0 \quad \triangle \]
\[ x/\theta_0 = 300.0 \quad \square \]
\[ x/\theta_0 = 392.2 \quad \diamond \]
\[ U^+ = y^+ \]
\[ U^+ = 2.44 \ln y^+ + 5.0 \]

We = 75 Newtonian
\[ x/\theta_0 = 88.28 \quad \bullet \]
\[ x/\theta_0 = 200.0 \quad \triangle \]
\[ x/\theta_0 = 300.0 \quad \square \]
\[ x/\theta_0 = 392.2 \quad \diamond \]
\[ U^+ = y^+ \]
\[ U^+ = 2.44 \ln y^+ + 5.0 \]

We = 100 Newtonian
\[ x/\theta_0 = 88.28 \quad \bullet \]
\[ x/\theta_0 = 200.0 \quad \triangle \]
\[ x/\theta_0 = 300.0 \quad \square \]
\[ x/\theta_0 = 392.2 \quad \diamond \]
\[ U^+ = y^+ \]
\[ U^+ = 2.44 \ln y^+ + 5.0 \]

Figure 4. Profiles of streamwise mean velocity in wall units: (a) We = 25, (b) We = 50, (c) We = 75 and (d) We = 100.

behaviour. This observation is related to the phase difference between streamwise profiles of the drag reduction ratio and streamwise turbulence intensity as further discussed below (see figure 9c for details).

Figure 5(d) also shows that at We = 100 a second maximum appears around \( y^+ = 200 \), and the second maximum values are almost independent of the streamwise location. This second peak rises due to the strong suppression of \( u'_{rms} \) in the log layer and seems to be consistent with experimental measurements on drag-reduced turbulent boundary layer for dilute cationic surfactant solutions, in which the second peak is observed near the centre of the boundary layer (see Itoh et al. 2005; Tamano et al. 2009b). These authors claimed that the second peak is due to the formation of the shear-induced structure (SIS), which is strongly related to the viscoelasticity and the drag-reducing ability in the turbulent flow of the dilute cationic surfactant solution. However, the second peak here may be due to long relaxation time, since the present DNS does not take the structure modification such as the SIS into account. Thus, further investigations are needed to understand the origin of the second peak of the streamwise turbulence intensity.
Figure 5. Profiles of streamwise turbulence intensity in wall units: (a) $We = 25$, (b) $We = 50$, (c) $We = 75$ and (d) $We = 100$.

Figure 6 shows distributions of the wall-normal turbulence intensity $v'_{rms}$ in wall units. For all of the cases of $We$, the wall-normal turbulence intensity $v'_{rms}$ is smaller than that for the Newtonian fluid. At the same streamwise location, the maximum of $v'_{rms}$ becomes smaller with the increase in $We$. At $We = 75$ and 100, the maxima of $v'_{rms}$ are almost half those of the Newtonian fluid. The maxima of $v'_{rms}$ also move away from the wall; the maxima at $We = 50–100$ are located at $y^+ \simeq 200$, while the maximum at $We = 25$ is located at $y^+ \simeq 100$.

Figure 7 shows distributions of the Reynolds shear stress $-u'v'$. At $We = 25$, $-u'v'$ is slightly smaller than that of Newtonian fluid. As a whole, $-u'v'$ decreases with the increase in $We$. At $We = 75$ and 100, the Reynolds shear stress is weak across the boundary layer in the downstream region. This is consistent with experimental results that the Reynolds shear stress is very small at large drag reduction ratios for wall-bounded turbulent flows (see e.g. Warholic et al. 1999a,b; Kawaguchi et al. 2002; Itoh et al. 2005; Tamano et al. 2009b).

Figure 8 shows profiles of trace of the conformation tensor, $C_{kk}/L^2$. The maximum of $C_{kk}/L^2$ in the region of $10 < y^+ < 30$ indicates that turbulence statistics are strongly
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Figure 6. Profiles of wall-normal turbulence intensity in wall units: (a) $We = 25$, (b) $We = 50$, (c) $We = 75$ and (d) $We = 100$.

affected in the buffer layer by the high elongational viscosity. The value of $C_{kk}/L^2$ is almost zero in the region away from the wall. At the same streamwise location, the $C_{kk}/L^2$ becomes larger with the increase in $We$.

Next, we investigate streamwise profiles of turbulence statistics at $y^+ = 30$, since both their modification and the polymer elongation are largest in the vicinity of this value, as observed above. Figure 9(a–e) show streamwise variations in the mean velocity, trace of conformation tensor, streamwise turbulence intensity, wall-normal turbulence intensity and Reynolds shear stress, respectively. In figure 9(a), solid and dashed lines represent Virk and Newtonian log-laws, respectively. For the Newtonian fluid, mean velocities scaled by the friction velocity at $y^+ = 30$, $U^+|_{y^+ = 30}$ are almost constant and slightly smaller than the Newtonian log-law in the whole computational domain. For viscoelastic fluids, near the inlet region, $U^+|_{y^+ = 30}$ decreases in the streamwise direction, and has a minimum. This corresponds to the region of negative drag reduction and is again due to the inlet condition. Downstream of this region at $We = 25$, $U^+|_{y^+ = 30}$ has a maximum at $x/\theta_0 \simeq 150$ and a slight minimum at $x/\theta_0 \simeq 270$, and slightly increases again. At $We = 50$, $U^+|_{y^+ = 30}$ has a slight maximum in the region of $250 \leq x/\theta_0 \leq 300$. At $We = 75$ and 100, $U^+|_{y^+ = 30}$ gradually increases and reaches
the Virk log-law value. Streamwise profiles of $U^+|_{y^+=30}$ are similar with those of drag reduction ratio $DR$ (cf. figures 9a and 3).

Figure 9(b) shows that the maximum of $\overline{C_{kk}|_{y^+=30}}/L^2$, which is observed near $x/\theta_0 = 50$, increases with the increase in $We$. Note that streamwise locations of maxima of $\overline{C_{kk}|_{y^+=30}}/L^2$ correspond to locations of minima of $DR$. Downstream of such maxima, at $We = 25$, $\overline{C_{kk}|_{y^+=30}}/L^2$ has a slight minimum at $x/\theta_0 \simeq 180$ and a slight maximum at $x/\theta_0 \simeq 300$. At $We = 50, 75, 100$, $\overline{C_{kk}|_{y^+=30}}/L^2$ decreases in the streamwise direction, while $U^+|_{y^+=30}$ or $DR$ increases. This indicates that once polymers are strongly stretched in the upstream region, which results in the high extensional viscosity, large viscoelastic stress is not necessary for the large $DR$ in the downstream region. We elaborate on this observation below. It is also reminiscent of the observation by Xi & Graham (2010b) in minimal channel flow that during intervals of ‘hibernation’, in which the level of drag reduction is highest, the polymer chains are relaxing. That is, what occurs temporally in the minimal channel is similar to what occurs spatially in boundary layer flow. The connection between these observations is particularly close in the $We = 25$ case, where the level of drag reduction displays

Figure 7. Profiles of Reynolds shear stress in wall units: (a) $We = 25$, (b) $We = 50$, (c) $We = 75$ and (d) $We = 100$. 

\begin{figure} 
\centering 
\subfloat[]{
\includegraphics[width=0.4\textwidth]{figure7a}
\caption{(a) $We = 25$ Newtonian DNS by Spalart ($Re_\theta = 670$)}
\label{fig:7a}
\endfloat 
\hfill
\subfloat[]{
\includegraphics[width=0.4\textwidth]{figure7b}
\caption{(b) $We = 50$ Newtonian DNS by Spalart ($Re_\theta = 670$)}
\label{fig:7b}
\endfloat 
\hfill
\subfloat[]{
\includegraphics[width=0.4\textwidth]{figure7c}
\caption{(c) $We = 25$ Newtonian DNS by Spalart ($Re_\theta = 670$)}
\label{fig:7c}
\endfloat 
\hfill
\subfloat[]{
\includegraphics[width=0.4\textwidth]{figure7d}
\caption{(d) $We = 25$ Newtonian DNS by Spalart ($Re_\theta = 670$)}
\label{fig:7d}
\endfloat 
\end{figure}
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both a maximum, at $x/\theta_0 \approx 160$, and a minimum, at $x/\theta_0 \approx 260$. The level of polymer stretching has corresponding extrema a short distance downstream, i.e. a minimum at $x/\theta_0 \approx 180$ and a maximum at $x/\theta_0 \approx 280$. The present result is also consistent with the DNS of Dimitropoulos et al. (2005) and the experiment of Hou et al. (2008).

It can be observed that the streamwise profile shifts downstream as $We$ increases (figure 9c). At $We = 25$, the streamwise location at which $u_{rms}^{+} | y^{+} = 30$ of viscoelastic fluids becomes larger than that of Newtonian fluid shifts downstream compared with the streamwise location at which the $DR$ becomes positive. The same behaviour is observed at $We = 50$ and higher. Moreover, such phase difference between $DR$ and $u_{rms}^{+} | y^{+} = 30$ increases with the increase in $We$, i.e. the relaxation time $\lambda$. The lack of correspondence of $DR$ and $u_{rms}^{+} | y^{+} = 30$ observed here is consistent with the first DNS of Dimitropoulos et al. (2005) who reported that the phase difference between polymer stretch and vortex damping increased with $We$.

Figure 9(d) shows that the wall-normal turbulence intensity at $y^{+} = 30$, $u_{rms}^{+} | y^{+} = 30$, sharply decreases as $We$ increases. At $We = 25$, $u_{rms}^{+} | y^{+} = 30$ starts to increase at $x/\theta_0 \approx 100$, reaches the maximum at $x/\theta_0 \approx 230$ and then slightly decreases in the streamwise
direction. At $We = 50$, $v'_{rms} | y^+ = 30$ gradually increases from $x/\theta_0 \simeq 200$, while at $We = 75$ and 100, it very slightly increases from around $x/\theta_0 = 350–380$, respectively. The streamwise profiles of $v'_{rms} | y^+ = 30$ seem to be shifted more downstream compared with those of $u'_{rms} | y^+ = 30$. This can be seen for example by the fact that the maximum of $v'_{rms} | y^+ = 30$ is more downstream than that of $u'_{rms} | y^+ = 30$.

Figure 9(e) shows the Reynolds shear stress $-\overline{u'v'} | y^+ = 30$. Its qualitative behaviour is similar to that of $v'_{rms} | y^+ = 30$. At $We = 100$, the $-\overline{u'v'} | y^+ = 30$ is very small in $100 < x/\theta_0 < 200$, and is slightly increasing with downstream distance. The small value of the Reynolds shear stress has been reported in experimental studies on drag-reducing cationic surfactant solutions (see e.g. Warholic et al. 1999b; Kawaguchi et al. 2002; Itoh et al. 2005; Tamano et al. 2009b) and polymer solutions (Warholic et al. 1999a).
Comparing streamwise variations among the drag reduction ratio $DR$, trace of conformation tensor, and turbulence statistics (cf. figures 3 and 9), it is revealed that the trace of conformation tensor, i.e. the magnitude of polymer elongation is anticorrelated with $DR$. On the other hand, compared with the streamwise profile of $DR$, streamwise profiles of streamwise and wall-normal turbulence intensities and the Reynolds shear stress shift downstream, and the phase difference becomes larger with the increase in $We$, in which the phase difference from $DR$ is largest for the wall-normal intensity and is smallest for the streamwise turbulence intensity.

To clarify the dependence on the relaxation time $\lambda$ of the streamwise variations of turbulence statistics, the abscissa in figure 9, $x/\theta_0$, is replaced by $x/\theta_0/We$ in figure 10. With this change, we are measuring downstream distance in length travelled per polymer relaxation time. When viewed this way it is seen that the variations in streamwise and wall-normal turbulence intensities and the Reynolds shear stress at
different We are comparable, unlike in figure 9. In particular, the positions of the extrema on figure 10 display a much weaker dependence on We than on figure 9. This observation indicates that the phase difference observed here is mainly due to the difference in the relaxation time.

4.3. Correlations between stress, velocity and polymer conformation

The results above show a general trend of the level of drag reduction (or, equivalently, the mean velocity at \( y^+ = 30 \)) increasing while the polymer stress decreases. As noted, this observation is generally consistent both with some previous work on boundary layers (Dimitropoulos et al. 2005) and the observations of Xi & Graham (2010b) in minimal channel flow, although the present results are somewhat influenced by the artificial inlet boundary condition. In this section we examine in more detail the relationship between wall shear stress, velocity and polymer conformation.

Figure 11 shows instantaneous contours of local wall-shear stress fluctuation \( \tau''_w = \tau_w - \bar{\tau}_w z \) scaled by \( \bar{\tau}_w z \). Black and white contours represent high and low wall-shear stress regions, respectively. For the Newtonian fluid, many small high and low wall-shear stress regions appear. On the other hand, at \( We = 25 \), high and low wall-shear stress regions show larger scales. At \( We = 50 \), some high wall-shear stress regions are observed and the instantaneous wall-shear stress is almost homogeneous in the downstream region. At \( We = 75 \) and 100, the local wall-shear stress is almost uniform except in the upstream region, where the influence of the artificial inlet boundary condition is large.

To examine the relationships between velocity, wall-shear stress and polymer conformation in more detail, we present in figure 12 joint probability density functions (JPDFs) of instantaneous wall-shear stress \( \tau_w / (\rho U^*_e) \) and streamwise velocity scaled by friction velocity \( U^{++} \) at wall normal position \( y^{++} = 30 \) in the whole computational domain. Figure 12(a–c) reveal that the correlation between \( \tau_w / (\rho U^*_e) \) and \( U^{++} |_{y^{++}=30} \) is negative, and the strongest correlation is observed around the Newtonian log-law line for the Newtonian fluid, in the region between the Virk and Newtonian log-
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Figure 12. Joint probability density functions of instantaneous wall-shear stress and streamwise velocity scaled by friction velocity at $y^{++} = 30$ in the whole computational domain: (a) Newtonian, (b) $We = 25$ and (c) $We = 50$.

The Newtonian log-law lines at $We = 25$, and around the Virk log-law line at $We = 50$. Figure 13 shows JPDFs of instantaneous trace of conformation tensor $C_{kk}/L^2$ at $y^{++} = 30$ and $U^{++}|_{y^{++}=30}$ in the whole computational domain. The negative correlation between $C_{kk}|_{y^{++}=30}/L^2$ and $U^{++}|_{y^{++}=30}$ is observed at both $We = 25$ and 50. Figure 14 shows JPDFs of instantaneous wall-shear stress $\tau_w/(\rho U_e^2)$ and trace of conformation tensor $C_{kk}/L^2$ at $y^{++} = 30$ in the whole computational domain. One can confirm the positive correlation between $\tau_w/(\rho U_e^2)$ and $C_{kk}|_{y^{++}=30}/L^2$ at both $We = 25$ and 50, which is consistent with the finding that $U^{++}|_{y^{++}=30}$ is negatively correlated to both $C_{kk}|_{y^{++}=30}/L^2$ and $\tau_w/(\rho U_e^2)$.

Figure 15 shows values of $U^{++}|_{y^{++}=30}$ versus $\tau_w/(\rho U_e^2)$ at a particular time instant at $z = 3L_c/4$, i.e. along a line oriented in the streamwise direction. For the Newtonian case, these ‘trajectories’ show movement with a negative correlation over a wide range of $U^{++}|_{y^{++}=30}$ and $\tau_w/(\rho U_e^2)$. At $We = 25$, the trajectories are confined to a smaller range of $\tau_w/(\rho U_e^2)$. At $We = 50$, the range of $U^{++}|_{y^{++}=30}$ is almost the same as in the
Figure 13. Joint probability density functions of instantaneous trace of conformation tensor and streamwise velocity scaled by friction velocity at $y^{+} = 30$ in the whole computational domain: (a) $We = 25$ and (b) $We = 50$. Note the change in the horizontal axis scale between the two plots.

Figure 14. Joint probability density functions of instantaneous wall-shear stress and trace of conformation tensor at $y^{+} = 30$ in the whole computational domain: (a) $We = 25$ and (b) $We = 50$.

Newtonian case, but there is much less (spatial) fluctuation. Figure 16 shows values of $U^{+} |_{y^{+}=30}$ versus $C_{kk} |_{y^{+}=30}/L^2$ as a function of $x$ at $z = 3L_z/4$. It is found that at $We = 50$ the movement is less and the range is wider than at $We = 25$.

The results presented here clearly indicate a local negative correlation between the level of drag reduction (mean velocity) and polymer stress, and are again consistent with the presence of the active and hibernating turbulence mechanism in the turbulent boundary layer flow.
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Figure 15. Instantaneous values of $U^{++}|_{y^{++}=30}$ versus $\tau_w/(\rho U_e^2)$ as a function of $x$ at $z = 3L_e/4$: (a) Newtonian, (b) $We = 25$ and (c) $We = 50$. Symbols $\bigcirc$, $\vartriangle$ and $\square$ illustrate the values at $x/\theta_0 = 100, 200$ and $300$, respectively.

4.4. Effect of removal of polymer stresses in downstream region

To further examine the role of the viscoelastic stresses in the downstream evolution of the level of drag reduction, we performed simulations at $We = 100$ in which the viscoelastic stresses were set to zero beyond a fixed downstream distance $b$. Two values of $b$ were tested: $b = 100\theta_0$, where the polymer stretching and turbulence intensity are large and the level of drag reduction is slightly negative (because of the inlet conditions), and $b = 200\theta_0$, where the polymer stress is still substantial but the level of drag reduction is high. The removal of the stresses was implemented by multiplying them by the damping function,

$$W(x) = \frac{1}{2} \left[ 1 - \frac{\tanh \left\{ \frac{\alpha(x - b)}{1 - 2b} \right\} \tanh(\alpha)}{(1 - 2b)x + b} \right],$$

(4.2)
Figure 16. Instantaneous values of $U^{+}|y^{++}=30$ versus $C_{kk}|y^{++}=30/L^2$ as a function of $x$ at $z = 3L_z/4$: (a) $We = 25$ and (b) $We = 50$. Symbols $\bigcirc$, $\triangle$ and $\square$ illustrate the values at $x/\theta_0 = 100$, 200 and 300, respectively.

where $\alpha$ is fixed at 50. All other numerical and physical conditions are the same as in the previous sections.

Figure 17(a–f) show the streamwise dependence of the trace of conformation tensor $\overline{C_{kk}}|y^{++}=30/L^2$, the drag reduction ratio $DR$, the mean velocity $U^{+}|y^{++}=30$, the streamwise and wall-normal turbulence intensities $u'_{rms}|y^{++}=30$ and $v'_{rms}|y^{++}=30$, and the Reynolds shear stress $-\overline{u'v'^{+}}|y^{++}=30$ in these cases.

Consider first the case of damping at $x/\theta_0 = 100$. The streamwise profile of $DR$ starts to depart from the profile without damping at $x/\theta_0 = 80$ and reaches a maximum around $x/\theta_0 = 130$, in which the value is more than twice the value of $DR$ without damping at the same streamwise location (figure 17b). The sudden change of the momentum balance (removal of the polymer contribution to the shear stress) causes the large drag reduction around $x/\theta_0 = 130$, which corresponds to the maximum of $U^{+}|y^{++}=30$ (see also figure 17c).

After the maximum, the level of $DR$ drastically decreases, becoming negative and almost constant in the region of $280 \leq x/\theta_0 \leq 400$ (figure 17b). This rapid reversion to essentially normal Newtonian turbulence does not seem to be linked to outer region dynamics as these are hardly affected at all by the polymer dynamics. This point is illustrated in figure 18, which suggests that the difference in outer region turbulence statistics with and without damping is small.

Now consider the case of damping at $x/\theta_0 = 200$, where there is already a substantial degree of drag reduction. As in the above case, there is a slight increase in the level of drag reduction due to removal of the polymer shear stresses, but in contrast to that case, the level of drag reduction now remains high in the remainder of the domain. Similarly, $U^{+}|y^{++}=30$ with damping at $x/\theta_0 = 200$ is larger than without damping (cf. figures 17b and 17c). These results support the hypothesis that once the flow has been driven by polymer stretching into a regime with substantial drag reduction, the viscoelastic stress is not necessary for the drag reduction to persist for a substantial distance in the downstream region. (Of course, one expects that in a sufficiently long domain the flow would eventually revert...
back to conventional Newtonian turbulence.) Analogous results were found in the minimal channel simulations of Xi & Graham (2010b). They observed that once the a viscoelastic simulation had begun to enter a hibernation interval, the polymer stresses could be turned off and the flow would continue to hibernate for several eddy turnover times, exhibiting for example the same transient approach to the Virk log-law slope found in the fully viscoelastic case.

Values of $u'^+_{rms}|_{y^+=30}$, $v'^+_{rms}|_{y^+=30}$ and $-u'v'^+_{rms}|_{y^+=30}$ with damping at $x/\theta_0 = 100$ have maxima at $x/\theta_0 = 200$, 250 and 220, respectively, which are much larger than in the Newtonian case, and then decrease to the outlet plane. At $x/\theta_0 > 300$, they are almost constant and $u'^+_{rms}|_{y^+=30}$ and $-u'v'^+_{rms}|_{y^+=30}$ are slightly smaller than that in the Newtonian case. On the other hand, with damping at $x/\theta_0 = 200$, the $u'^+_{rms}|_{y^+=30}$ and $v'^+_{rms}|_{y^+=30}$ increase monotonically from $x/\theta_0 \simeq 180$ to the outlet plane, at which $u'^+_{rms}|_{y^+=30}$ is almost twice that of Newtonian fluid, while $v'^+_{rms}|_{y^+=30}$ and $-u'v'^+_{rms}|_{y^+=30}$ are still smaller than those of Newtonian fluid. These increases in the
velocity fluctuations are consistent with expectation mentioned above that far enough downstream, the turbulence will revert to normal.

5. Conclusions

DNS of a zero-pressure gradient drag-reducing turbulent boundary layer of a viscoelastic fluid were performed at the momentum–thickness Reynolds number $Re_\theta = 500$ and Weissenberg numbers $We = 25, 50, 75$ and $100$ using the FENE-P model with the maximum chain extensibility parameter $L^2 = 10000$ and the ratio of solvent viscosity to zero shear rate solution viscosity $\beta = 0.9$. An important limitation of the present study (as with many previous studies of boundary layer flow) is the artificial inlet condition. This condition leads to substantial transient stretching of the polymers and correspondingly to a negative level of drag reduction in the upstream region of the flow. (This condition is somewhat similar to the case of injecting polymers into an established turbulent boundary layer.) On the other
hand, most of the key qualitative results of this work arise from observations of the dynamics well downstream of this region, as well as trends with increasing $We$ that are expected to be independent of the details of the upstream conditions. Key observations include the following. As $We$ increases, i.e. the relaxation time becomes longer, the streamwise profile of $DR$ shifts downstream. Here $DR$ increases with the streamwise location, while the trace of conformation tensor decreases. More generally, the trace of conformation tensor, i.e. the magnitude of polymer elongation is spatially anticorrelated with $DR$, while in terms of streamwise and wall-normal turbulence intensities and the Reynolds shear stress, the phase difference from $DR$ becomes larger with the increase in $We$, in which such the difference is largest and smallest for the wall-normal and streamwise turbulence intensities, respectively. The relationship between polymer stretching, velocity and wall shear stress was further illustrated by examination of joint probability density functions of instantaneous values of these quantities. These results shed further light on the spatial anticorrelation between polymer stretching and drag reduction as well as showing a related anticorrelation between the mean velocity at the edge of the log layer and the wall shear stress. Finally, by performing simulations in which the polymer stress is set to zero beyond a given downstream position, it is shown that high levels of drag reduction can be maintained for some distance downstream in the absence of polymer stress.

These results are consistent with recent observations by Xi & Graham (2010b) in minimal channel flow of viscoelastic fluids, and suggest that an important role for viscoelasticity in the turbulent drag reduction phenomenon, at least near solid surfaces, is to suppress conventional turbulence, while leaving behind a much weaker form of turbulence that can persist for a substantial length of time (or downstream distance) even in the absence of viscoelastic stresses.

This work was carried out under the Excellent Young Researchers Overseas Visit Program of the Japan Society for the Promotion of Science. It was partially supported by a Grant-in-Aid for Scientific Research (grant numbers 18360087 and 21760126) from the Japan Society for the Promotion of Science. MDG acknowledges the support of the National Science Foundation (grant number CBET-1066223).

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